

## Estimation of Groundwater Seepage Risks into Tunnel Using Radial Basis Function Networks

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### Abstract

In this study, Site Groundwater Rating (SGR) in the Amirkabir tunnel has been estimated using Radial Basis Function Networks (RBFNs). SGR is the first rating method that by considering the parameters like joint frequency, joint aperture, schistosity, crashed zones, karstification, soil permeability coefficient, tunnel location in the water table or piezometric surface, and the amount and intensity of annual raining in the area, classifies the tunnel path from the risk of groundwater seepage point of view. In this article, using an RBFN, an estimation of SGR along the Amirkabir tunnel path was performed. Field data obtained from primary studies in the tunnel was used to train and test the prepared network. For the testing set, modeling results showed that SGR could be predicted with the mean error of 3.57% and 4.76% using radial basis network and exact radial basis network functions, respectively. A High correlation between the SGR of the tunnel path and the network answers, confirmed the prepared RBFN.

### Introduction

One of the problems of tunnels is the penetration of groundwater by engineers and workers, which creates significant risks and incidents (Maleki et al., 2022). The presence of groundwater reduces the stability of tunnel walls and roofs and, in some cases, causes severe and sudden flooding, leading to heavy losses and damage. It is impossible to determine all the efficient factors of water flow in a tunnel. Therefore, it seems complicated to accurately predict the rate of leakage. The analytical methods and equations have many applications in the calculation of water penetration rates in tunnels due to their simplification and the use of practical theory (Farhadian et al., 2021). In recent decades, scientists have tried to

provide increasingly sophisticated analytical solutions to estimate the groundwater penetration into tunnels. (Agatonovic-Kustrin and Beresford 2000, Farhadian et al., 2016a). Among the most important researches on calculating water seepage into the tunnel, Goodman et al. (1965), Freeze and cherry (1979), Lei (1999), Karlsrud (2001), Lombardi (2002), and EL Tani (1999 & 2003), Perrochet and Dematteis (2007), Park et al. 2008, Gattinoni et al. 2008, Moon and Fernandez (2009), Farhadian and Katibeh (2017) and Maleki (2018) can be mentioned. The evaluation of the tunnel sections due to the risk of groundwater inflow was discussed. The analytical formulas are derived to simplify the geostructural configuration, and the input data are kept as

simple as possible. An analytical solution is used to predict the groundwater flow into the tunnel based on simplified assumptions (Farhadian et al., 2016b):

1. 2-D flow and circular tunnel cross-section,
2. Homogenous and isotropic permeability,
3. The tunnel section is located under water table.

Groundwater inflow to the tunnel is one of the perilous conditions in the time of excavating underground tunnels. One of the dangerous conditions when excavating underground tunnels. The problem of groundwater penetration is very difficult to control. This is due to the fact that the prediction of low flows results in high costs and unsafe operating conditions. The high flow encourages contractors to ignore it. There are basically two problems with flow prediction. The first is that no satisfactory solutions have been proposed so far in the literature on the groundwater flow into hard rock tunnels. (Farhadian and Nikvar Hassani, 2019). The second problem is the wide variation of permeability along the tunnel section, sometimes up to six orders of magnitude. It is the responsibility of the tunnel designer to estimate the amount and location of groundwater entering the tunnel (Nikvar Hassani et al., 2016, Palmstrom and Stille, 2007, Sievanen, 2001).

An overall assessment of the groundwater inflow to the tunnel provides the basis for the designation of a drainage system. Groundwater intrusion affects both construction methods and plans. Therefore, minor errors in flow prediction can lead to long delays in comparing progress with excessive and unnecessary costs. In hard rock tunnels, it is the characteristics of the inflow that most of the inflow occurs in a few places; however, some of the inflow comes from many places. Therefore, most of the tunnel is dry. The total flow is obtained by adding the flow velocity along the length of the tunnel. This is a common phenomenon observed in hard rock tunnel projects and is the leading cause of many problems in estimating groundwater flow using standard hydrogeological solutions. (Moon and Fernandez, 2010, Butscher, 2012, Farhadian et al., 2016, Nikvar Hassani et al., 2018).

Several factors influencing the infiltration of groundwater into groundwater have been identified: (Farhadian et al., 2017):

- The size and dimension of an excavation/tunnel/water conductive zone,
- Depth of the underground excavation below the groundwater table,
- Groundwater recharge,
- Hydraulic conductivity of the rock mass/water conductive zone (geological and structural conditions).

Of the above parameters, the most important parameter in calculating the groundwater flowing in the tunnel is the permeability of the bedrock (before and after grouting) (Farhadian and Katibeh, 2015a, Brantberger et al., 1998). In addition, it has been statistically proven that the composition and thickness of the overburden play a decisive role in the water penetration rate. (Cesano, 1999, Cesano et al., 2000). However, Polla and Ritola (1989) found no correlation between excavation volume and water inflow rate. It should be noted, however, that Farhadian et al. (2016) argued that the volume of excavation (tunnel radius) plays an important role in tunneling groundwater into solid rock masses. In addition, an unpublished literature review of groundwater penetration in excavations Tolppanen, (1997) indicates that because the quantitative values cannot be compared directly due to different uses and methods of excavation, the researcher found a very weak correlation between the volume of excavation and inflow rate. In general, the existence of a weak correlation between the above parameters can be explained by the fact that in hard crystalline rock tunnels, most flows usually take place at relatively small spots or lines in the crushed zone and fractured area. (Moon and Jeong, 2011, Farhadian and Katibeh, 2015b, Moeini et al., 2018).

Recently, the use of artificial neural networks has greatly increased the hydrogeological debate, and many researchers predict various topics, such as groundwater levels, flow, and transport (Daliakopoulos et al., 2005; Lallahem et al., 2005; Rajurkara et al., 2004; Morshed and Kaluarachchi, 1998; Imrie et al., 2000; Kompani-Zare and Zhan, 2006; Gunnink et

al., 2012). Mathematical attribute models (Li et al., 2013; Wang et al., 2012), analytic hierarchical processes Ren and Xu (2011), and fuzzy extension theory Li et al., (2015) are various probabilistic mathematical techniques which widely used to assess the risk of water inflow to tunnels and coal mines. In general, the evaluation results are at an acceptable level, but subjectivity exists in the weights and scales of the evaluation indicators.

In addition, some computer intelligence techniques, such as artificial neural networks, support vector machines, and Gaussian processes, have been used to analyze landslides Grelle and Guadagno, (2013), deformation of surrounding rocks Feng et al (2004), and surface deposition. Suwansawat and Einstein, (2006); Ovidio et al., (2008), pipe failure rates Tabesh et al., (2009); Shirzad et al., (2014) and other geotechnical issues (Ocak and Seker, 2012). Several related studies have also used artificial neural networks and support vector machines to predict mine leaks, and water flows in tunnels Guo and Ma, (2010); Ren and Xu, (2011). In this study, RBFN has been used to predict SGR for the first time.

## Materials and Methods

### Site Groundwater Rating

Based on the preliminary studies of the tunnel sites, for the first time, Katibeh and Aalianvari (2009) provided the SGR method for dividing the tunnel path to different rates regarding the risk of groundwater seepage. In this rating system, from groundwater seepage point of view, the tunnel path is divided to 6 No risk, Low risk, Moderate risk, Risky, High risk, and Critical classes by considering parameters like joints frequency and aperture, schistosity, crashed zones, karstification, soil permeability coefficient, tunnel location in the water table or piezometric surface, and annual raining. Based on this method, the total score of the site, SGR, is calculated from the following equation (1) (Katibeh and Aalianvari, 2009):

$$\text{SGR} = [(S_1 + S_2 + S_3 + S_4) + S_5] S_6 S_7 \quad (1)$$

where,

$S_1$  is the score of frequency and aperture of joints which is obtained using the following equation (2):

$$S_1 = 25 \times \left( \sum_{i=1}^n \frac{\lambda_i g e_i^2}{12\nu} a \right) \quad (2)$$

which,  $\lambda_i$  is the joint frequency (1/m),  $g$  is the earth's gravity ( $\text{m sec}^{-2}$ ),  $e_i$  is the mean hydraulic joint aperture (m),  $\nu$  is the kinematic viscosity of water ( $\text{m}^2 \text{sec}^{-1}$ ), and  $a$  is the unit factor ( $\text{sec m}^{-1}$ ) for conversion of  $S_1$  to dimensionless form.

$S_2$  is the score of schistosity and ranged between 1 and 5 according to the degree of schistosity.

$S_3$  is the score of the crashed zone and is calculated based on crashed zone width using Table (1).

$S_4$  is the karstification score and is based on the intensity of karstification ranging from 10 to 100.  $S_5$  is the soil permeability score.  $S_5$  is calculated as follows:

$$S_5 = K \times C \quad (3)$$

where,  $K$  is the soil permeability (m/day), and  $C$  is the unit factor (day/m) for conversion of  $S_5$  to dimensionless form.  $S_6$  is the score of the water head above the tunnel.  $S_6$  is obtained using equation (4):

$$S_6 = \frac{H}{\ln(H \times d)} \times d \quad (4)$$

where,  $H$  is the water head above the tunnel and  $d$  is the unit factor (1/m) for conversion of  $S_6$  to dimensionless form.

$S_7$  is the annual raining score.  $S_7$  can be obtained by means of equation 5 regarding annual raining.

$$S_7 = \frac{P_y}{5000} \quad (5)$$

where,  $P_y$  is annual raining (mm).

**Table 1- Equations for computation of  $S_3$  (Katibeh and Aalianvari, 2009)**

Type of rock	Crashed zone width	$S_3$
Clay base rocks	CZW	$2 \times \text{Log}(10\text{CZW} \times b)$
Other rock types	CZW	$100 \times \text{Log}(10\text{CZW} \times b)$

In comparison with earthen sites, parameters like crashed zone, joint frequency, and karstification have more significance in earthen sites. By contrast, in earthen sites, permeability coefficient is more important, while in rocky media, this factor is determined by frequency and aperture of joints. Therefore, in rocky site  $S_5$  and in earthen site  $S_1$  to  $S_4$  are assumed to be zero. Moreover, if the tunnel is excavated in unsaturated media,  $S_6$  will be considered as unit. Also, in areas that are unsaturated, annual precipitation is a factor that is important when drilling tunnels. If the tunnel is drilled in a saturated area, it is assumed to be a unit.

After the calculation of SGR coefficients for the intended sections in the tunnel, there must exist a criterion to evaluate the amount and size of this coefficient, based on which groundwater seepage risk into the tunnel (with a qualitative and quantitative view) can be evaluated. Predicting the rate of inflow water into the tunnel can cause the appropriate designing of drainage systems and even choosing the most appropriate excavation method, so the required preparations are performed to prevent possible risks. This was suggested based on the amounts of water inflow in Table (2) (Farhadian et al., 2012).

The larger the SGR coefficient, the more the permeated water amount to the tunnel (at least in a short time) and therefore, drainage tools and methods must be stronger and more expensive. Even sometimes, tunnel excavation methods must be revised so that the possibility of sudden and damaging incidents occurrence is decreased.

#### **Artificial Neural Networks**

An artificial neural network (ANN) is a digitized model of the human brain and a computer program that simulates how the human brain processes information. Like humans, ANNs are learned (or trained) by observing and experimenting with relevant examples of training, not programming (Agatonovic-Kustrin and Beresford, 2000).

ANNs are computing algorithms that mimic the four essential functions of these biological neurons. These functions take inputs from other neurons or sources, combine them, operate on results, and display the final result (Klerfors, 1998). What makes ANNs interesting is that once the network is set up, it can learn in a self-constructive way that mimics brain functions, such as pattern recognition, classification, and optimization (Haykin, (1994); Fausett, (1994); Klerfors, (1998); Kung, (1993); Tarassenko, (2004).

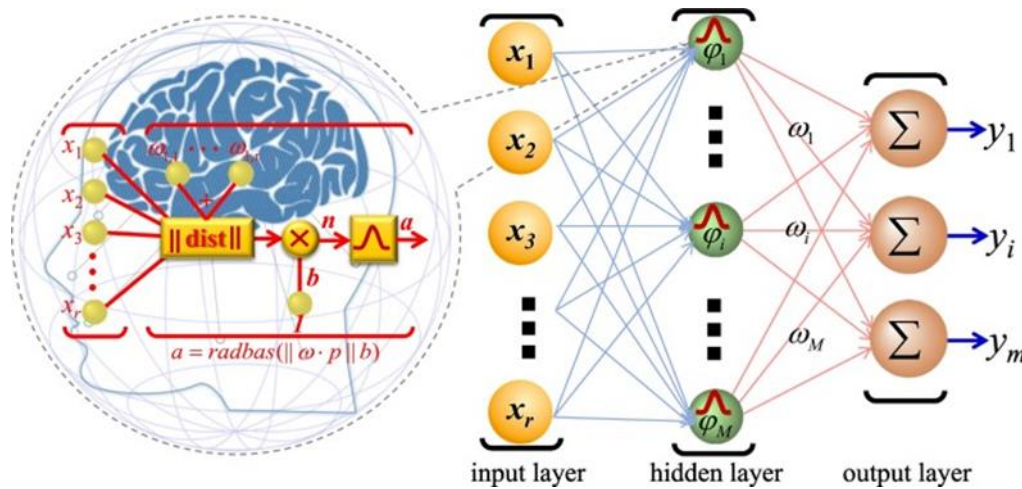
ANNs were first developed in the 1940s (Lin and Chen, 2004). ANNs paid a lot of attention to various fields of study and, they are used in statistical science, engineering, computer science, artificial intelligence, etc. Much effort has been made to find practical methods for understanding the structure of systems or processes that use ANNs. There is a lot of literature on neural networks, both theoretical and practical, and a wide range of practical applications of the technique (Bishop (1995); Ripley (1996); Sato (1996) and Webb (1999). In the field of ANNs, multilayer perceptrons and RBFNs have emerged as multilayer networks (Broomhead and Lowe, 1988). In particular, the RBFN, a hybrid learning method that combined self-organized learning and supervised learning, has recently attracted attention (Moody and Darken, 1989). RBFN models built with hybrid learning methods have important advantages over multilayer perceptrons: faster convergence and no identification problems.

#### **The Radial Basis Function Networks**

RBFNs were first introduced in 1988 (Broomhead and Lowe, 1988). The basic architecture of an RBFN is shown in Fig. (1). An RBFN has three layers, including an input layer, a hidden layer and, an output layer. The input layer is composed of input data. The hidden layer transforms the data from the input space to the hidden space using a non-linear function. The output layer, which is linear, yields the response of the network.

**Table 2- Qualitative and quantitative rating of tunnels site regarding water seepage based on SGR coefficient (Katibeh and Alianvari, 2009)**

SGR	Tunnel rating	Class	Probable conditions for groundwater inflow into tunnel (L/sec/min)
0 - 100	I	No risk	0 - 0.04
100 - 300	II	Low risk	0.04 - 0.1
300 - 500	III	Moderate risk	0.1 - 0.16
500 - 700	IV	Risky	0.16 - 0.28
700 - 1000	V	High risk	Q > 0.28 Inflow of groundwater and mud from crashed zones is probable
1000 <	VI	Critical	Inflow of groundwater and mud is highly probable



**Fig. 1-The structure of RBFN (Deng et al. 2021)**

In the structure of RBFNs, the input data X is an I-dimensional vector, which is transmitted to each hidden unit. The activation function of hidden units is symmetric in the input space, and the output of each hidden unit depends only on the radial distance between the input vector X and the center for the hidden unit (Lin and Chen, 2004). Different activation functions have been proposed for the hidden-layer neurons, but normally the selected one is the Gaussian function. In this paper, the Gaussian functions are applied as activation functions of the hidden layer neurons. There are six basic functions, which are recognized as having useful properties for RBFNs (Bishop, 1995; Hardy, 1971; Harpham and Dawson, 2006; Mai-Duy and Tran-Cong, 2003):

1. Multiquadratic :

$$\phi(\mathbf{x}) = (x^2 + \sigma^2)^{1/2}, \tag{6}$$

Which is a case of

$$\phi(\mathbf{x}) = (x^2 + \sigma^2)^\alpha \quad 0 < \alpha < 1, \tag{7}$$

2. Gaussian:

$$\phi(\mathbf{x}) = \exp\left(-\frac{x^2}{2\sigma^2}\right), \tag{8}$$

3. Inverse multiquadratic :

$$\phi(\mathbf{x}) = (x^2 + \sigma^2)^{-\beta}, \quad \beta > 0. \tag{9}$$

4. Thin plate spline:

$$\phi(\mathbf{x}) = \left(\frac{x}{\sigma}\right)^2 \ln\left(\frac{x}{\sigma}\right). \tag{10}$$

5. Cubic:

$$\phi(\mathbf{x}) = x^3. \tag{11}$$

6. Linear:

$$\phi(\mathbf{x}) = x, \quad (12)$$

Where  $\phi(\mathbf{x})$  is the basis function,  $\sigma$  is the width of the basis function,  $x = \|\mathbf{x} - \mathbf{c}_k\|$ , where  $\mathbf{x}$  is the training data,  $\mathbf{c}_k$  is the center of the  $k$ th neuron in hidden layer and,  $\|\cdot\|$  is the Euclidean norm.

The RBFN, a class of single hidden layer feedforward networks, is expressed as a linear combination of radially symmetric nonlinear basis functions and takes the following form:

$$u(\mathbf{x}) = \sum_{k=1}^m W_k \phi_k(\mathbf{x}) + w_0 \quad (13)$$

Where  $\phi_k(\mathbf{x})$  is the response of the hidden neuron.  $W_k$  is the connecting weight between the  $k$ th hidden neuron and the output unit,  $w_0$  is the bias term, and  $u(\mathbf{x})$  is the output of the network.

In the Learning Phase of the RBFNs, the center and width are decided first. It takes advantage of the well-defined meanings of the RBFN parameters. The centers are highly related to the density of data points. Without using the class label, K-means is the most typical method to divide the samples into different clusters (Kiernan et al., 1996; Mendoza et al., 2009; Moody, 1991; Moody and Darken, 1989). It minimizes the distance between the center and the samples in that cluster. Since the class label is available in a classification problem, the supervised method could be used. Learning Vector Quantization (LVQ) algorithm was proposed by Kohonen for vector quantization and classification tasks (Vogt, 1993; Kohonen, 1990). Different from unsupervised clustering, each cluster center belongs to a class. A center is moved closer to samples in the same class and away from samples belonging to a different class. The decision tree can be used to separate the feature space into different regions. Each region represents the center of the RBFN (Kubat, 1998; Yoo and Sethi, 1995).

The next step is the selection of the width for each center. The width can be determined by computing the variance of all samples in a

cluster (Brizzotti and Carvalho, 1999; De Castro et al., 1999). K-nearest-neighbor algorithm is sometimes applied, and the width is calculated as the mean of distances among the centers belonging to other K-nearest hidden neurons (Mak and Cho, 1998; Musavi et al., 1992; West and Dellana, 2009). The next phase is to find the weights after the centers and widths are decided. They can be easily found by linear optimization using any linear least-squares methods. Gradient Descent and Singular Value Decomposition (SVD) are two popular methods (Kiernan et al., 1996; Bruzzone and Prieto, 1999; Mak and Cho, 1998).

### Case Study: Amirkabir Tunnel

Amirkabir tunnel, located northwest of Tehran, Iran, is designed and being operated to transfer water from the Amirkabir dam to Tehran. One of the difficulties in this project is groundwater inflow into the tunnel while doing the excavation operations. In this study, SGR for this tunnel was predicted using RBF networks.

### Geology of the Area

In the performed geological studies, the tunnel was divided into 14 different geological units that generally encompass various sedimentary-volcanic sets from the Karaj formation. Its petrology generally includes an alteration of tuff, sandstone, fine-grained conglomerates, and siltstone, lava and, agglomerate parts. In this study, we deal with investigating the SGR from kilometers 3.1 to 14.1 of the tunnel. As shown in Fig. (2), it is divided into 9 geological engineering sections, Gta2 (sandstone and tuff layers), Gta3 (sandstone layers, tuff, and micro conglomerate), Gta4-1 (sandstone, tuff), Gta4-2 (tuff, in sandstone sections and micro conglomerate), Sts1 (tuff, siltstone, layers of sandstone and micro conglomerate), Sts2-1 (tuff, limestone), Sts2-2 (tuff, limestone, shale and siltstone), Tsh-1 (Sandstone, Shale, Siltstone), and Cz (tuff, sandstone, and micro conglomerate) (SCE Company, 2006) (Fig. 2).

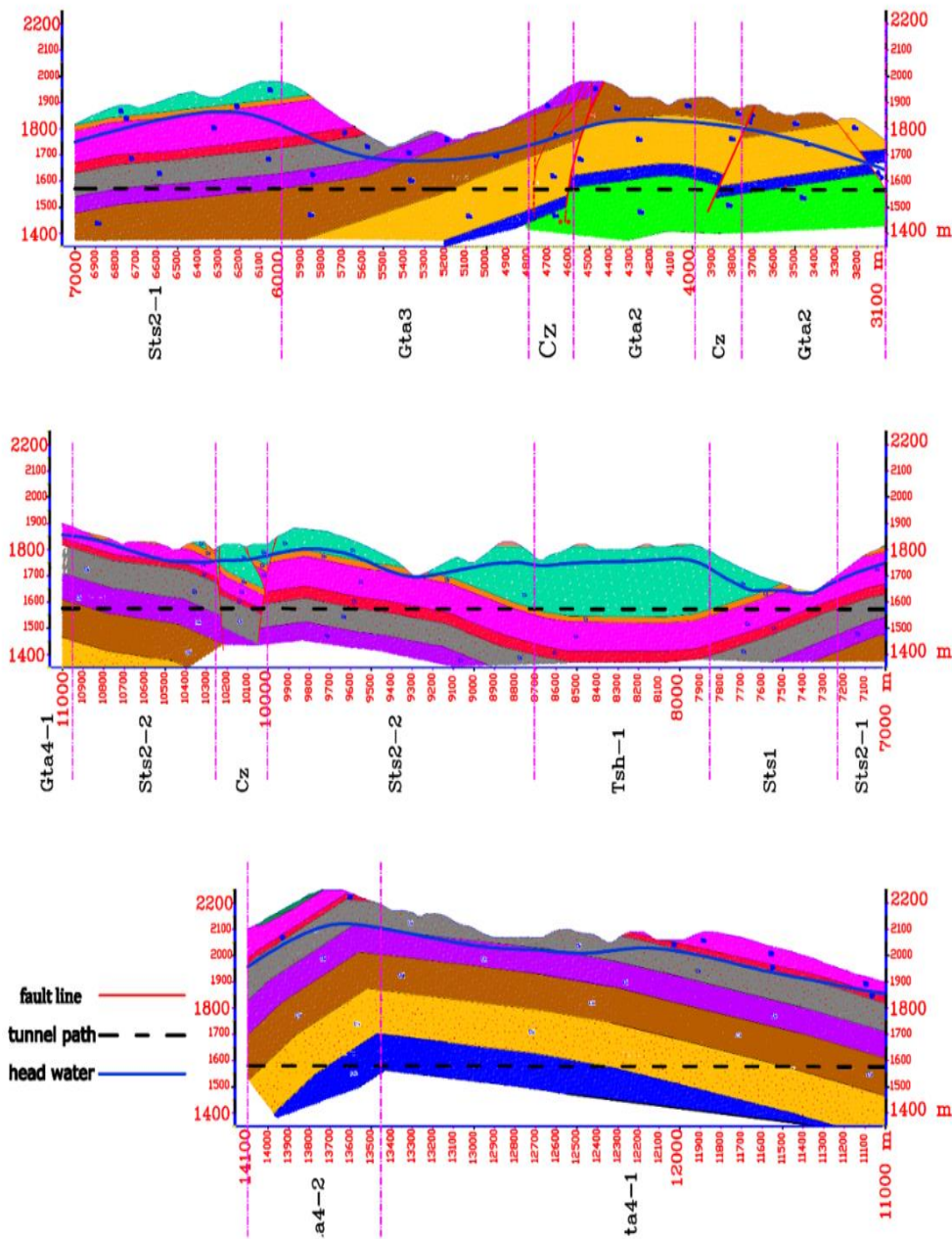


Fig. 2- Geological sections of Amirkabir tunnel (km 3.1 to 14.1) (SCE Company, 2006).

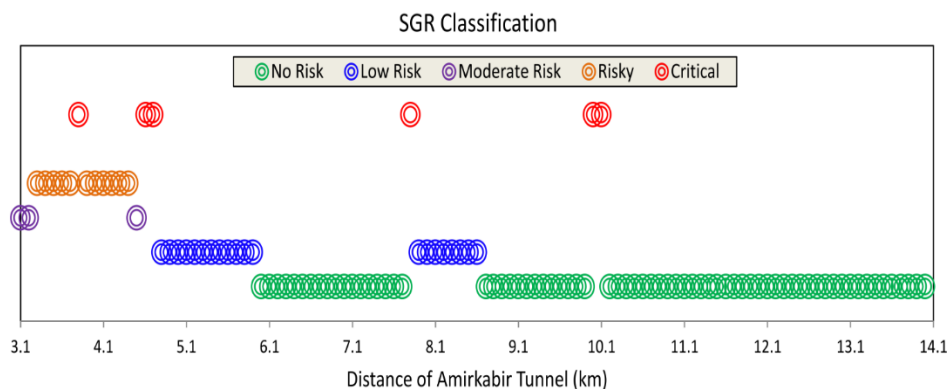
**Rating of Amirkabir Tunnel Site (in terms of groundwater seepage hazards based on SGR coefficient)**

Field data obtained from the Amirkabir tunnel showed two sets of joints in the rock mass. Considering parameters like joint aperture, tunnel's excavation depth, the width of crashed zones, and height of groundwater table above the tunnel axis, SGR coefficients are calculated in 110 sections of the tunnel

path (each 100 meters), the summary of which is shown in Table 3 and Fig. (3). As obtained from the results, SGR method divides the tunnel path to 5 various rates regarding groundwater seepage hazard. Among 110 excavated sections in the tunnel path, 70 sections are located in No risk, 20 sections in Low risk, 3 sections in Moderate risk, 11 sections in risky, and 6 sections in critical class.

**Table 3- Classification of 110 excavated sections in Amirkabir tunnel path from kilometers 3.1 to 14.1 based on groundwater seepage hazard by SGR method.**

water inflow risk	Number of section	length (m)	%
No risk	70	6920	63
Low risk	20	2110	19
Moderate risk	3	310	3
Risky	11	1140	10
High risk	0	0	0
Critical	6	520	5
summation	110	11000	100



**Fig. 3- Classification of 110 excavated sections in Amirkabir tunnel path from kilometers 3.1 to 14.1 based on groundwater seepage hazard by SGR method**

#### The proposed RBF model

In this study, using MATLAB software, an RBFN was designed to predict SGR. Because rock type of the Amirkabir tunnel site, parameters like joint aperture, joint frequency and karstification are concerned.  $S_5$ , permeability coefficient parameter was considered zero because this parameter is hidden in rock media, joints frequency, and their aperture, and other factors. The amount and intensity of annual raining in the area is concerned when the tunnel is excavated in the unsaturated zone, so because the Amirkabir tunnel is located in the saturated zone from kilometer 3.1 to 14.1, the score of this factor was considered 1, automatically. On the other hand, due to the lack of schistosity and karstification outcrop in the tunnel path, the coefficient of these two parameters in all the sections was considered zero. Consequently, joint frequency, joint aperture, JRC, JCS of each set of joints, water head, overburden, and the score of crashed zones ( $S_3$ ) were selected as the network's input parameters, and various SGR classes were considered as output. The data used for training and testing

the prepared network was acquired from the primary studies in the Amirkabir tunnel. The optimum network was constructed by testing several models and repeating them. Each ANN was trained with 3/4 of the data set, and remaining was used to evaluate their accuracy and trend stability. The values of each class and the class frequency for SGR classification in all data and training data are shown in Fig. (4). A preprocessing of input and output data was performed, and they were normalized between [-1, 1] thereafter. In order to normalize the data, the following formula was used:

$$x = 2 \frac{x - \min x}{\max x - \min x} - 1 \quad (14)$$

It is clear that after finishing the simulation, the converse of the above functions were exerted. The learning rate of the network was measured by target functions during the learning process. At last, the network with the least error and highest regression coefficient was selected. The network error was calculated through the following equation:



Network error for training data (testing) = {number of training data (testing) which are not located in their own class/ total number of used data for training (testing)}.

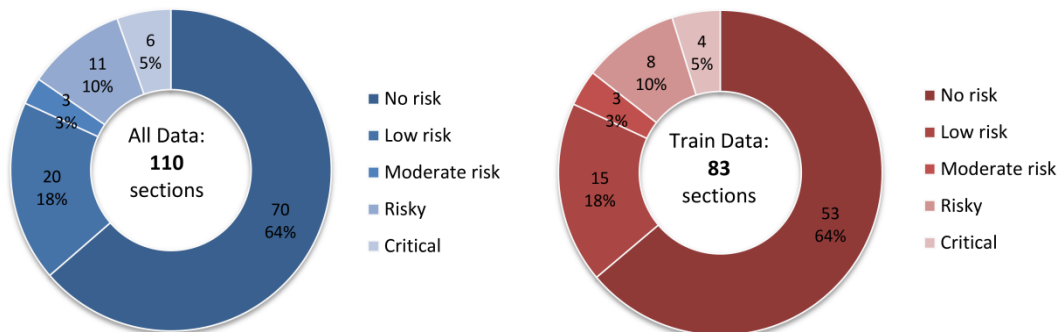
Due to random selection of the training and testing data and also network weights, the results were different. All networks were operated 10 times, and the average was considered as the final result.

**Results and Discussions**

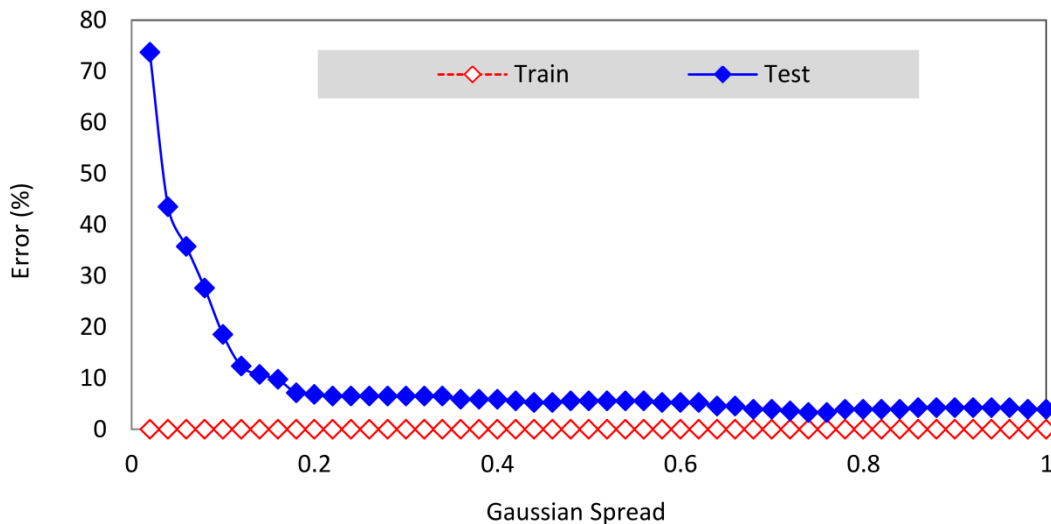
After the determination of network structure, SGR was predicted.

**Gaussian Spread Determination**

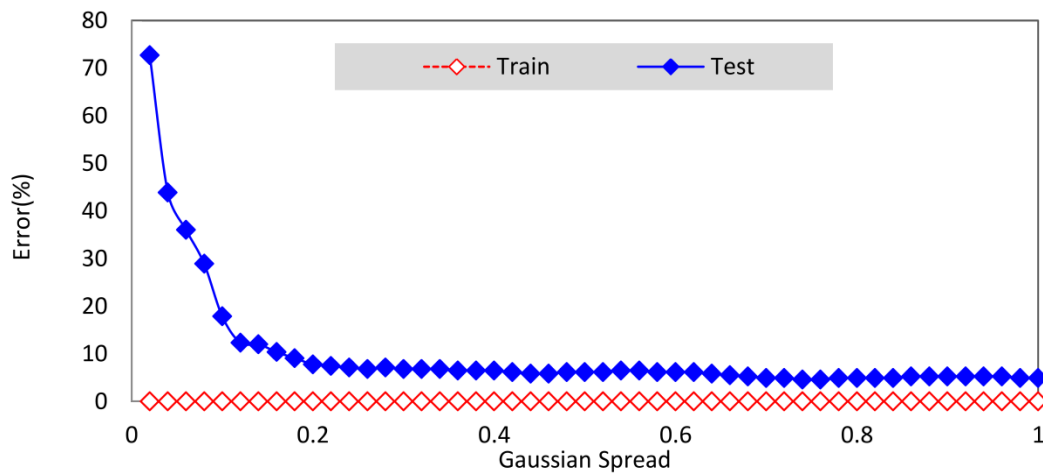
One of the most important issues in the design of RBFNs is Gaussian spread determination. MATLAB software uses newrb and newrbe functions for constructing an RBFN. This process was performed by newrb and newrbe functions. To determine optimal Gaussian spread, several networks with variable spread values from 0 to 1 and 0.02 spacing were constructed. Fig. (5) and (6) show the percentage mean value of network error after 10 runs related to the Gaussian spread values of the newrb and newrbe functions.



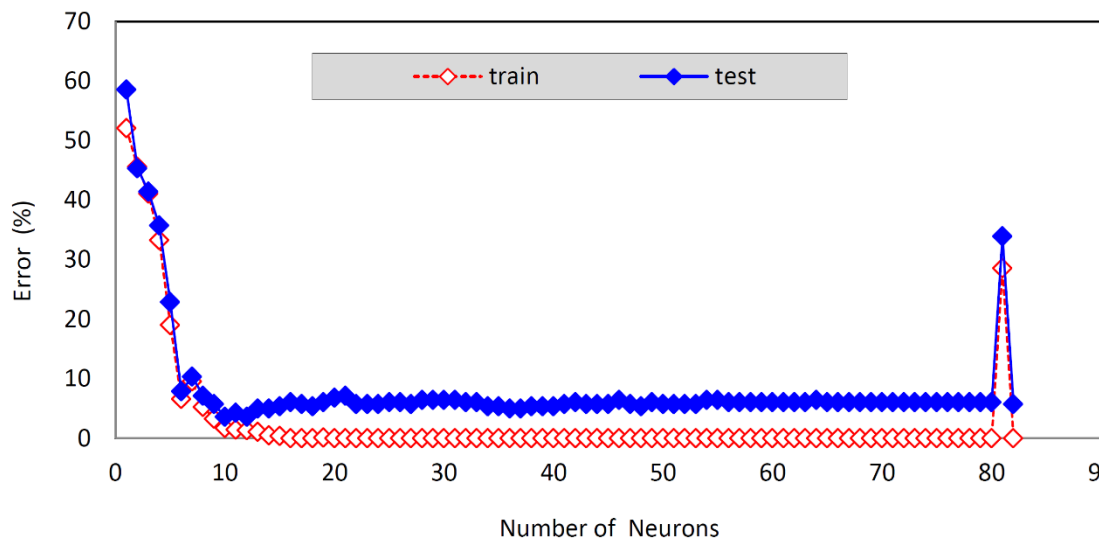
**Fig.4- Analysis of each class and the class frequency for SGR classification in all data and training data**



**Fig. 5- The percentage of the mean value of network error related to the amounts of Gaussian spread (newrb function)**



**Fig. 6-** The percentage of the mean value of network error related to the amounts of Gaussian spread (newrbe function)



**Fig. 7-** The percentage of the mean value of network error related to the neurons' number of the hidden layer

As observed in Fig. 5 and Fig. 6, with a Gaussian spread of 0.74, the least error occurred for structured networks by newrb and newrbe functions.

#### **Influence of Neurons' Number of the Hidden Layer in Network Error:**

As mentioned, the application of the newrb functions is a method for constructing RBF networks. Adding neurons into the RBF network consecutively, this process continued until the error was less than the goal value or reached to maximum determined neurons' number (total numbers of training data). In contrast, the neurons' number of newrbe function was constant and equal to the total number of training data. In

this study, the influence of neurons' number of the hidden layer on the network's error was investigated by newrb function. Fig. (7) shows the percentage of the mean value of network error after 10 runs related to the neuron's number of network hidden layer.

As observed in Fig. (7), with a network including 12 neurons in the hidden layer, the least error occurred for training and testing sets.

#### **Optimal Network**

After performing the above stages, the networks with the Gaussian spread value of 0.74 were constructed and by which SGR was modeled. Considering the selection of random training and testing data and

thereupon the weights, network error values in every run were different. Table 4 contains data about the percentage of minimum, maximum, and mean network error values after 10 runs.

The performance of the trained network was investigated by Regression analysis. To do so, network output and target vector were given to the postreg function. As a result, this function gave three parameters, two of which were m and b calculated from slope and intercepts of plot the network output vs. target vector. The third variable returned by postreg was the correlation coefficient between outputs and targets. The higher correlation coefficient the more compatible of predicted data and target vector and the more performance of the network (Demuth and Beale, 1998). Fig. (8) shows the

regression analysis resulted from modeling SGR for test data.

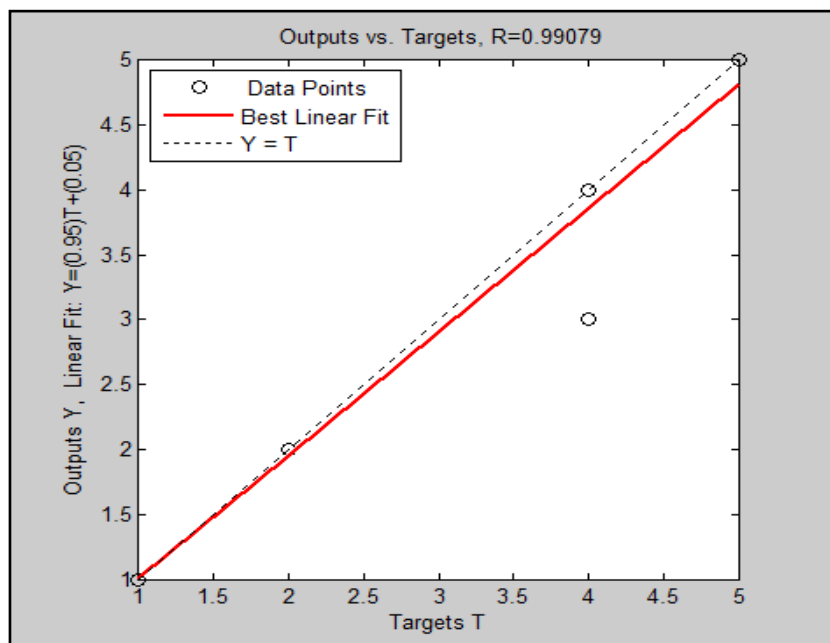
Fig. (8) shows the SGR classification (measured data) and predicted this classification for testing data (using RBF). According to this figure, the coefficient of correlation ( $R^2$ ) of the RBFN model is 0.9931. This high coefficient of correlation shows the accordance between the results of the RBFN model and measured data. Also, the following values are obtained as the output of the postreg function:

- Slope: 0.99
- Y-intercept: 0.051

Regarding regression analysis resulted values, it can be concluded that a perfect compatibility exists between the results obtained from the proposed RBFN and SGR.

**Table 4- Network errors for training and testing data**

Data set	training data (newrb function)	testing data (newrb function)	training data (newrbe function)	testing data (newrbe function)
Minimum network error (%)	0	0	0	0
Maximum network error (%)	2.44	10.71	0	7.14
Mean of network error (%)	1.42	4.76	0	3.57



**Fig. 8- Regression analysis resulted from modeling SGR for testing data**

## Conclusion

In this study, RBFN was used to predict the SGR for the Amirkabir tunnel. In addition, network structure and the optimum network were also determined. Distance between the joints, joint aperture, JRC and JCS of each joint set, water head, overburden and score of crashed zones ( $S_3$ ) were selected as input parameters, while various SGR classes were considered as network output. The data required for network training were obtained from preliminary studies in the path of the Amirkabir tunnel. The results of this

research showed that with the help of an RBFN, SGR could be predicted well. Also, high regression analysis proves the very good conformity between results gained from SGR and predicted by the RBFN.

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## Reference

- 1- Agatonovic-Kustrin S, and Beresford R. 2000. Basic concepts of artificial neural network (ANN) modeling and its application in pharmaceutical research. *Journal of pharmaceutical and biomedical analysis*, 22(5), pp.717-727.
- 2- Bishop C.M. 1995. *Neural Networks for Pattern Recognition*. Oxford University Press, *Oxford*.
- 3- Brantberger M., Dalmalm T., Eriksson M., Stille H. 1998. Steering factors of tightness around a pregrouted tunnel. Royal Institute of Technology, Stockholm, Sweden. In Swedish.
- 4- Brizzotti M.M., Carvalho A.C.P.L.F. 1999. The influence of clustering techniques in the RBF networks generalization: Proceedings of the Seventh International Conference on Image. *Processing and Its Applications 1*, pp. 87–92.
- 5- Broomhead D.S., Lowe D. 1988. Multivariable functional interpolation and adaptive networks. *Complex Sys.* 2, pp. 321-335
- 6- Bruzzone L., Prieto D.F. 1999. A technique for the selection of kernel-function parameters in RBF neural networks for classification of remote-sensing images. *IEEE. Trans. Vol. Geosci. & Remote Sen.* 37 (2), pp. 1179–1184.
- 7- Butscher, C., 2012. Steady-state groundwater inflow into a circular tunnel. *Tunnelling and Underground Space Technology*, 32, pp.158-167.
- 8- Cesano D. 1999. *Prediction of Groundwater flows into Underground Constructions in Hard Rocks*. Royal Institute of Technology, Stockholm, Sweden.
- 9- Cesano D., Olofsson B., Bagtzoglou A.C. 2000. Parameters Regulating Groundwater inflows into Hard Rock Tunnels - a Statistical Study of the Bolmen Tunnel in Southern Sweden. *Tunneling and Underground Space Technology*, 15(2):153-165.
- 10-Daliakopoulos, I.N., Coulibaly, P. and Tsanis, I.K., 2005. Groundwater level forecasting using artificial neural networks. *Journal of hydrology*, 309(1-4), pp.229-240.
- 11-De Castro, M.C.F., De Castro, C.C. and Arantes, D.S., 1999, July. RBF neural networks with centers assignment via Karhunen-Loeve transform. In *IJCNN'99. International Joint Conference on Neural Networks. Proceedings (Cat. No. 99CH36339)* (Vol. 2, pp. 1265-1270). IEEE.
- 12-Demuth H., Beale M. 1998. *Neural Network Toolbox for Use with Matlab*, Fifth ed. Math works.
- 13-Deng Y., Zhou X., Shen J., Xiao G., Hong H., Lin H., Wu F. and Liao B.Q. 2021. New methods based on back propagation (BP) and radial basis function (RBF) artificial neural networks (ANNs) for predicting the occurrence of halo ketones in tap water. *Science of The Total Environment*, 772, p.145534.

- 14-El Tani M. 1999. Water inflow into tunnels. Proceedings of the World Tunnel Congress ITA- ITES 1999, Oslo, pp. 61–70, Balkema.
- 15- El Tani M. 2003. Circular tunnel in a semi-infinite aquifer. *Tunn. Undergr. Space Technol.* 18 (1), pp. 49-55.
- 16-Farhadian H. and Nikvar-Hassani A. 2019. Water flow into tunnels in discontinuous rock: a short critical review of the analytical solution of the art. *Bulletin of Engineering Geology and the Environment*, 78(5), pp.3833-3849.
- 17-Farhadian, H., Aalianvari, A. and Katibeh, H., 2012. Optimization of analytical equations of groundwater seepage into tunnels: A case study of Amirkabir tunnel. *Journal of the Geological Society of India*, 80(1), pp.96-100.
- 18-Farhadian H., Katibeh H., 2015a. Groundwater Seepage Estimation into Amirkabir Tunnel Using Analytical Methods and DEM and SGR Method. World Academy of Science, Engineering and Technology, International Journal of Civil, Structural, *Construction and Architectural Engineering*, 9(3):296-301.
- 19-Farhadian H., Katibeh H., 2015b. Effect of Model Dimension in Numerical Simulation on Assessment of Water Inflow to Tunnel in Discontinues Rock. World Academy of Science, Engineering and Technology, International Journal of Environmental, Chemical, Ecological, Geological and *Geophysical Engineering*, 9(4):350-353.
- 20-Farhadian H., Katibeh H., Huggenberger P., Butscher C. 2016a. Optimum model extent for numerical simulation of tunnel inflow in fractured rock. *Tunnelling and Underground Space Technology*, 60:21-29.
- 21-Farhadian, H., Katibeh, H. and Huggenberger, P., 2016b. Empirical model for estimating groundwater flow into tunnel in discontinuous rock masses. *Environmental Earth Sciences*, 75(6), pp.1-16.
- 22-Farhadian, H., Nikvar Hassani, A. and Katibeh, H., 2017. Groundwater inflow assessment to Karaj Water Conveyance tunnel, northern Iran. *KSCE Journal of Civil Engineering*, 21(6), pp.2429-2438.
- 23-Farhadian, H., Salehzadeh, M.H. and Nikvar-Hassani, A., 2021, June. Model dimension effect in DEM and FEM simulations for assessment of water inflow into a tunnel. In *55th US Rock Mechanics/Geomechanics Symposium. OnePetro*.
- 24-Fausett, L., 1994. Fundamentals of Neural Networks. Prentice Hall International. Inc.: *Upper Saddle River, NJ, USA*.
- 25-Feng X.T., Zhao H. and Li S. 2004. Modeling non-linear displacement time series of geo-materials using evolutionary support vector machines. *International journal of rock mechanics and mining sciences*, 41(7), pp.1087-1107.
- 26-Fernandez G., Moon J. 2010. Excavation-induced hydraulic conductivity reduction around a tunnel, part 1: guideline for estimate of ground water inflow rate. *Tunn Undergr Space Technol* 25(5):560-566.
- 27-Freeze R.A., Cherry J.A. 1979. Groundwater: Prentice-Hall, Englewood Cliffs, New Jersey.
- 28-Gattinoni, P., Scesi, L.T.G. and Terrana, S., 2008. Hydrogeological risk analysis for tunneling in anisotropic rock masses. In *ITA-AITES World Tunnel Congress* (pp. 1736-1747).
- 29-Goodman, R.E., Moya, D.G., Van Schalkwyk, A. and Javandel, I., 1964. *Ground water inflows during tunnel driving*. College of Engineering, University of California.
- 30-Grelle, G. and Guadagno, F.M., 2013. Regression analysis for seismic slope instability based on a double phase viscoplastic sliding model of the rigid block. *Landslides*, 10(5), pp.583-597.
- 31-Xiaohui, G.U.O. and Xiaoping, M.A., 2010. Mine water discharge prediction based on least squares support vector machines. *Mining Science and Technology (China)*, 20(5), pp.738-742.

- 32-Gunnink J.L., Bosch J.H.A., Siemon B., Roth B., Auken E. 2012. Combining ground-based and airborne EM through Artificial Neural Networks for modelling glacial till under saline groundwater conditions. *Hydrology & Earth System Sciences*, 16 (8), pp. 3061-3074. 14p.
- 33-Hardy, R.L., 1971. Multiquadric equations of topography and other irregular surfaces. *Journal of geophysical research*, 76(8), pp.1905-1915.
- 34-Harpham, C. and Dawson, C.W., 2006. The effect of different basis functions on a radial basis function network for time series prediction: A comparative study. *Neurocomputing*, 69(16-18), pp.2161-2170.
- 35- Haykin, S., 1994. Neural networks: MacMillan College Publ. Co., New York.
- 35-Imrie, C.E., Durucan, S. and Korre, A., 2000. River flow prediction using artificial neural networks: generalisation beyond the calibration range. *Journal of hydrology*, 233(1-4), pp.138-153.
- 36-Karlsruh K. 2001. Water control when tunnelling under urban areas in the Oslo region. NFF publication No. 12, 4, 27–33, NFF.
- 37-Katibeh, H. and Aalianvari, A., 2009. Development of a New Method for Tunnel Site Rating from. *Journal of Applied Sciences*, 9(8), pp.1496-1502.
- 38-Kiernan, L., Mason, J.D. and Warwick, K., 1996. Robust initialisation of gaussian radial basis function networks using partitioned k-means clustering. *Electronics letters*, 32(7), pp.671-673.
- 39-Klerfors, D. and Huston, T.L., 1998. Artificial neural networks. *St. Louis University, St. Louis, Mo.*
- 40-Kohonen T. 1990. The self-organizing map: Proc. *IEEE*. 78 (9), pp. 1464–1480.
- 41-Kompani-Zare, M. and Zhan, H., 2006. Steady flow to a horizontal drain in an unconfined aquifer with variable thickness. *Journal of hydrology*, 327(1-2), pp.174-185.
- 42-Kubat, M., 1998. Decision trees can initialize radial-basis function networks. *IEEE Transactions on Neural Networks*, 9(5), pp.813-821.
- 43-Kung, S.Y., 1993. Digital neural networks. *PTR Prentice Hall Englewood Cluffs.*
- 44-Lallahem, S., Mania, J., Hani, A. and Najjar, Y., 2005. On the use of neural networks to evaluate groundwater levels in fractured media. *Journal of hydrology*, 307(1-4), pp.92-111.
- 45-Lei, S., 1999. An analytical solution for steady flow into a Ttonnel. *Groundwater*, 37(1), pp.23-26.
- 46-Li L., Lei T., Li S., Zhang Q., Xu Z., Shi S. and Zhou, Z. 2015. Risk assessment of water inrush in karst tunnels and software development. *Arabian Journal of Geosciences*, 8(4), pp.1843-1854.
- 47-Li, S.C., Zhou, Z.Q., Li, L.P., Xu, Z.H., Zhang, Q.Q. and Shi, S.S., 2013. Risk assessment of water inrush in karst tunnels based on attribute synthetic evaluation system. *Tunnelling and underground space technology*, 38, pp.50-58.
- 48-Lin, G.F. and Chen, L.H., 2004. A non-linear rainfall-runoff model using radial basis function network. *Journal of Hydrology*, 289(1-4), pp.1-8.
- 49-Lombardi G. 2002. Private communication.
- 50-Mai-Duy, N. and Tran-Cong, T., 2003. Approximation of function and its derivatives using radial basis function networks. *Applied Mathematical Modelling*, 27(3), pp.197-220.
- 51-Mak, M.W. and Cho, K.W., 1998, May. Genetic evolution of radial basis function centers for pattern classification. In *1998 IEEE International Joint Conference on Neural Networks Proceedings. IEEE World Congress on Computational Intelligence (Cat. No. 98CH36227) (Vol. 1, pp. 669-673)*. IEEE.

- 52-Maleki, M.R., 2018. Groundwater Seepage Rate (GSR); a new method for prediction of groundwater inflow into jointed rock tunnels. *Tunnelling and Underground Space Technology*, 71, pp.505-517.
- 53-Maleki, Z., Farhadian, H. and Nikvar-Hassani, A., 2021. Geological hazards in tunnelling: the example of Gelas water conveyance tunnel, Iran. *Quarterly Journal of Engineering Geology and Hydrogeology*, 54(1).
- 54-Mendoza, O., Melin, P. and Licea, G., 2009. A hybrid approach for image recognition combining type-2 fuzzy logic, modular neural networks and the Sugeno integral. *Information Sciences*, 179(13), pp.2078-2101.
- 55-Moeini, H., Farhadian, H. and Nikvar-Hassani, A., 2018. Determination of the optimum sealing method for Azad pumped storage dam considering seepage analysis. *Arabian Journal of Geosciences*, 11(14), pp.1-13.
- 56-Moody, J.E., 1991, September. Note on generalization, regularization and architecture selection in nonlinear learning systems. In *Neural Networks for Signal Processing Proceedings of the 1991 IEEE Workshop* (pp. 1-10). IEEE.
- 57-Moody, J. and Darken, C.J., 1989. Fast learning in networks of locally-tuned processing units. *Neural computation*, 1(2), pp.281-294.
- 58-Moon, J. and Fernandez, G., 2010. Effect of excavation-induced groundwater level drawdown on tunnel inflow in a jointed rock mass. *Engineering Geology*, 110(3-4), pp.33-42.
- 59-Moon, J. and Jeong, S., 2011. Effect of highly pervious geological features on ground-water flow into a tunnel. *Engineering Geology*, 117(3-4), pp.207-216.
- 60-Morshed, J. and Kaluarachchi, J.J., 1998. Application of artificial neural network and genetic algorithm in flow and transport simulations. *Advances in Water Resources*, 22(2), pp.145-158.
- 61-Musavi, M.T., Ahmed, W., Chan, K.H., Faris, K.B. and Hummels, D.M., 1992. On the training of radial basis function classifiers. *Neural networks*, 5(4), pp.595-603.
- 62-Hassani, A.N., Farhadian, H. and Katibeh, H., 2018. A comparative study on evaluation of steady-state groundwater inflow into a circular shallow tunnel. *Tunnelling and Underground Space Technology*, 73, pp.15-25.
- 63-Nikvar Hassani A., Katibeh H., Farhadian H. 2016. Numerical analysis of steady-state groundwater inflow into Tabriz line 2 metro tunnel, northwestern Iran, with special consideration of model dimensions. *Bulletin of Engineering Geology and the Environment*. 75(4):1617-27.
- 64-Ocak, I. and Seker, S.E., 2012. Estimation of elastic modulus of intact rocks by artificial neural network. *Rock Mechanics and Rock Engineering*, 45(6), pp.1047-1054.
- 65-Ovidio J., Santos J.R., Tarcisio B.C. 2008. Artificial neural networks analysis of Sao Paulo subway tunnel settlement data. *Tunn. Undergr. Space Technol.* 23, 481–491.
- 66-Palmstrom, A. and Stille, H., 2007. Ground behaviour and rock engineering tools for underground excavations. *Tunnelling and Underground Space Technology*, 22(4), pp.363-376.
- 67-Park, K.H., Owatsiriwong, A. and Lee, J.G., 2008. Analytical solution for steady-state groundwater inflow into a drained circular tunnel in a semi-infinite aquifer: a revisit. *Tunnelling and Underground Space Technology*, 23(2), pp.206-209.
- 68-Perrochet, P. and Dematteis, A., 2007. Modeling transient discharge into a tunnel drilled in a heterogeneous formation. *Groundwater*, 45(6), pp.786-790.
- 69-Polla, J. and Ritola, J., 1989. Large rock caverns. Drainage and sealing of rock caverns. *Technical Research Centre of Finland, Research notes*, 1000.

- 70-Rajurkar, M.P., Kothiyari, U.C. and Chaube, U.C., 2004. Modeling of the daily rainfall-runoff relationship with artificial neural network. *Journal of Hydrology*, 285(1-4), pp.96-113.
- 71-Ren, R. and Xu, M., 2011. Using BP network to predict tunnel water-inrush in partition style anticlinal belt. *Xiandai Suidao Jishu*, 48(6), pp.47-52.
- 72-Ripley, B.D., 2007. *Pattern recognition and neural networks*. Cambridge university press.
- 73-Sato Y. 1996. On artificial neural networks as a statistical mode: Proc. Inst. Statist. Math. 44, pp. 85-98.
- 74-SCE Company 2006. Geological and Engineering Geological Report for Amirkabir Water Conveyance Tunnel Project (Lot1), unpublished report.
- 75-Shirzad A., Tabesh M. and Farmani R. 2014. A comparison between performance of support vector regression and artificial neural network in prediction of pipe burst rate in water distribution networks. *KSCE Journal of Civil Engineering*, 18(4), pp.941-948.
- 76-Sievanen U. 2001. Leakage and groutability. *Working Report 2001-06*.
- 77-Suwansawat, S. and Einstein, H.H., 2006. Artificial neural networks for predicting the maximum surface settlement caused by EPB shield tunneling. *Tunnelling and underground space technology*, 21(2), pp.133-150.
- 78-Tabesh M., Soltani J., Farmani, R. and Savic D. 2009. Assessing pipe failure rate and mechanical reliability of water distribution networks using data-driven modeling. *Journal of Hydroinformatics*, 11(1), pp.1-17.
- 79-Tarassenko L. 2004. A guide to neural computing applications: John Wiley & Sons.
- 80-Tolppanen, P., 1997. *Water Leakage amounts in excavations, literature study*. Memorandum T-2000-18/97 (based on a memorandum of 1996). Consulting Engineers Saanio & Riekkola Oy, Helsinki, Finland (in Finnish).
- 81-Vogt, M., 1993, March. Combination of radial basis function neural networks with optimized learning vector quantization. In *IEEE International Conference on Neural Networks* (pp. 1841-1846). IEEE.
- 82-Wang Y., Yang W., Li M. and Liu X. 2012. Risk assessment of floor water inrush in coal mines based on secondary fuzzy comprehensive evaluation. *International Journal of Rock Mechanics and Mining Sciences*, 52, pp.50-55.
- 83-Webb A. 1999. *Statistical Pattern Recognition*. Arnold, London.
- 84-West, D. and Dellana, S., 2009. Diversity of ability and cognitive style for group decision processes. *Information Sciences*, 179(5), pp.542-558.
- 85-Yoo J.H., Sethi I.K. 1995. Design of radial basis function networks using decision trees: Proceedings of the IEEE International Conference on Neural Networks 3, pp. 1269–1272.

